

- Ch-2:26 Add magnitudes of all right-ward forces and left-ward forces separately. Difference of total right-ward force and total left-ward force is net pull on the knot. Direction is easy to figure out.

- Ch-2:36

$$\vec{R} = \vec{A} + \vec{B} \quad (1)$$

Let's find out magnitude of vector  $\vec{R}$  in terms of magnitude of vector  $\vec{A}$  and  $\vec{B}$  and the angle between them.

$$\vec{R} \cdot \vec{R} = (\vec{A} + \vec{B}) \cdot (\vec{A} + \vec{B}) = A^2 + B^2 + \vec{A} \cdot \vec{B} + \vec{B} \cdot \vec{A} \quad (2)$$

where  $A = |\vec{A}|, B = |\vec{B}|$  is magnitude of vectors  $\vec{A}$  and  $\vec{B}$ . Dot product between vectors is commutative meaning  $\vec{A} \cdot \vec{B} = \vec{B} \cdot \vec{A}$

$$R^2 = A^2 + B^2 + 2AB \cos \phi \quad (3)$$

where  $\phi$  is the angle between the two vectors. As you can see  $0 \leq \phi \leq 180$  we have maximum magnitude when  $\phi = 0$  and minimum magnitude when  $\phi = 180$ .

- Ch-2:77 See solution to 36 for proof.
- Ch-2:88  $\phi = \arccos\left(\frac{R^2 - A^2 - B^2}{2AB}\right)$ . If  $|\vec{A} + \vec{B}| = 3$  then  $\phi = \arccos\left(\frac{3^2 - 4^2 - 5^2}{40}\right)$  similarly if  $|\vec{A} - \vec{B}| = 3$  then  $\phi = \arccos\left(\frac{3^2 - 4^2 - 5^2}{-40}\right)$
- Ch-4:34 (a)  $t = \sqrt{\frac{2 \cdot 0}{9.81}} = 0.45s$ , (b)  $v_x = \frac{3.0}{0.45} \frac{m}{s}$ , (c)  $v_{fy} = 0 - 9.81 \times 0.45 \rightarrow v = \sqrt{v_x^2 + v_f^2 y}$
- Ch-4:38 (a)  $t = \frac{16.7}{40} = 0.4175s$ , (b)  $\Delta y = \frac{1}{2}(9.81)(0.4175)^2$
- Ch-4: 40 Assume initial velocity  $v$  then  $v_x = v \cos 60, v_y = v \sin 60$  Time taken to travel  $6.1m$  horizontally is  $t = \frac{6.1}{v \cos 60}$ .  $y_f = 3.0m, y_o = 1.8m$

$$\text{Solve } 3.0 = 1.8 + v \sin 60 \left(\frac{6.1}{v \cos 60}\right) - \frac{1}{2}(9.81)\left(\frac{6.1}{v \cos 60}\right)^2$$

- Assume that  $x_o$  is the horizontal distance along the hill for the point where the projectile lands.

Solve  $y(t) = y_o + 75 \sin 60 t - \frac{1}{2}gt^2$  for  $y_o = 0$  and  $y_f = \tan 20(300 + x_o) - 109$ . Find time  $t_1, t_2$  in terms of  $x_o$ .

Time taken to travel horizontal distance  $300 + x_o$  is  $t = \frac{300 + x_o}{75 \cos 60}$ . Using  $t_2 = t$  find  $x_o$ . Rest is trivial.

#### Additional Problem

- (a)  $v_{ox} = 10 \cos 10, v_{oy} = 10 \sin 60$
- (b)  $v_x(t) = v_{ox}, v_y(t) = v_{oy} - gt$
- (c)  $x(t) = x_o + v_{ox}t, y(t) = y_o + v_{oy}t - \frac{1}{2}gt^2$  where  $y_o = 1.0m, g = 10$

(d) Solve for  $y(t) = 0$  let call the solution  $t_o$

(e) Use  $t_o$  from above and plug in  $x(t) = x_o + v_{ox}t$ .

(f) Use  $t_o$  to find  $v_y(t = t_o) = v_{oy} - gt_o$

$v = \sqrt{v_{ox}^2 + v_y^2(t = t_o)}$  and angle it makes with downward vertical  
is  $\theta = \arctan \frac{v_{ox}}{v_y(t=t_o)}$