Supplementary Figures: A random matrix definition of the boson peak

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Figure 1: 1/2 Definition (a) Low-frequency spectrum of the density of states $D(\omega)$ for jammed packings. Different colors correspond to different pressures ranging logrithmically from $10^{-1.4}$ to $10^{-4.8}$. Squares indicate the point where $D(\omega)$ reaches 1/2 of its maximum value, at a frequency $\omega_{1/2}^*(p)$ (b) Plot of $\log_{10} \omega_{1/2}^*(p)$, with best fit line of slope 0.47.



Figure 2: 1/4 Definition (a) Low-frequency spectrum of the density of states $D(\omega)$ for jammed packings. Different colors correspond to different pressures ranging logrithmically from $10^{-1.4}$ to $10^{-4.8}$. Squares indicate the point where $D(\omega)$ reaches 1/4 of its maximum value, at a frequency $\omega_{1/4}^*(p)$ (b) Plot of $\log_{10} \omega_{1/4}^*(p)$, with best fit line of slope 0.40.



Figure 3: $D(\omega)/\omega^{d-1}$ **Definition (a)** Low-frequency spectrum of the density of states divided by the Debye scaling in 2D $D(\omega)/\omega$ for jammed packings. Different colors correspond to different pressures ranging logrithmically from $10^{-1.4}$ to $10^{-4.4}$. Squares indicate the point where $D(\omega)\omega$ attains its maximum value, at a frequency $\omega_{max}^*(p)$ (b) Plot of $\log_{10} \omega_{max}^*(p)$, with best fit line of slope 0.38.



Figure 4: (a) Unscaled L_2 difference between eigenvector cdfs and the universal distribution for jammed packings as a function of frequency ω . Different colors correspond to different pressures ranging logarithmically from $10^{-1.4}$ to $10^{-4.2}$.